Numerical calculation of temperature sensing in seawater based on microfibre resonator by intensity-variation scheme

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A seawater temperature sensing and detection method based on microfibre resonator (MR) by intensity-variation scheme is proposed, which has the advantages of high sensitivity and low detection limit. The dependences of sensitivity on probing wavelength, fibre diametre and ring diametre are studied. Results show that probing wavelength influences the sensitivity by the absorption loss predominantly. Larger absorption loss results in lower sensitivity, which is much different with resonant-wavelength-shift scheme. And sensitivity increases with the increasing ring diametre due to the decreasing bending loss and increasing Q-factor. In addition, there may exist an optimal fibre diametre, with which the sensitivity is maximized. By tuning the parameters of system, sensitivity can be tuned from 0.0784 NI/°C to 13.79 NI/°C (NI is the abbreviation of normalized intensity). Correspondingly, dynamic range changes from 11.77°C to 0.08°C. Additionally, the dependences of detection limit on wavelength, fibre diametre, and ring diametre are also investigated, which are opposite to that of sensitivity. For different temperatures, the dependences of sensitivity and detection limit at some typical temperatures are studied, which shows that high sensitivity and low detection limit are related to high temperature, and the optimal fibre diameters for high sensitivity and low detection limit are the same at different temperatures. The lowest detection limit is estimated to be $10^{-7}$°C level, which is four orders of magnitude smaller than that of the traditional method. Results shown here are beneficial to find the optimal parameters for the temperature sensors, and offer helpful references for assembling micro-photonics device used in seawater sensing and detection.

Keywords: Microfibres, optical sensors, optical resonators, ring resonators, ocean temperature

1 INTRODUCTION

Seawater temperature is one of the most important parameters in oceanographic phenomena. For example, internal-wave phenomena happens accompany with seawater temperature fluctuation of about 1.5 – 3.5°C inevitably [1], which indicates that measuring temperature of seawater on line can detect the internal-wave phenomena effectively, and actually it is one of the most widely used methods for internal-wave detecting. Presently, the existing methods for seawater temperature measuring include conductivity-temperature-depth (CTD) system, microwave remote sensing, fibre brag grating and so on [2]–[4]. Among the above methods, CTD is the most popular equipment. However, due to the large size of CTD, the skin temperature of seawater cannot be measured precisely, which limits the application of CTDs in hydrospace detecting.

In recent years, sensors based on micro and nanofibres have attracted more and more attentions [5]–[28]. For temperature sensing and detection, sensors based on microfibre resonators (MRs) by resonant-wavelength-shift scheme have been investigated theoretically and demonstrated experimentally [29]–[33], which show sensitivity of 0.017 – 0.27 nm/°C. Expect for the resonant-wavelength-shift scheme, intensity-variation scheme can potentially provide a higher sensitivity and a simpler setup without the need of a spectrum measurement. But there is little study for the intensity-variation method [34]–[37]. Though for intensity-variation scheme it only functions when the monitoring wavelength lies close to the selected resonance, and this leads to a smaller dynamic range [38]. However, for temperature sensing in seawater the relative small dynamic range is wide enough.

In this paper, based on the MR by the intensity-variation scheme, a method for seawater temperature sensing and detection is proposed, which shows the advantages of high sensitivity and low detection limit. Combining the resonant theory of microfibre ring and empirical formula of seawaters refractive index, we investigate the dependence of transmission intensity on temperature. Then, the dependences of sensitivity on probing wavelength, fibre diametre and ring diametre are studied. Finally, we calculate the detection limit for typical probing wavelength, fibre diametre and ring diametre. Results presented here may offer helpful references for assembling micro-photonics device used in seawater sensing and detection.
2 MODELING AND THEORY

The schematic diagram of the seawater temperature sensing by intensity-variation system based on MR is shown in Figure 1, including optical source, optical spectrum analyzer, power meter, thermometer, temperature-controlled heating platform and 3dB coupler. Due to that in intensity-variation scheme, temperature change of seawater results in the RI changes of seawater and silica fibre, so we can realize the temperature sensing by monitoring the change of the transmission intensity around the resonant peak. The optical spectrum analyzer helps to find the resonant wavelength conveniently, once the probing wavelength is determined, seawater temperature sensing is mainly completed by monitoring the transmission intensity measured with the power meter.

The transmission intensity can be expressed as follows [39]:

\[
\tau = a^2 \frac{K + \sigma^2 - 2\sigma\sqrt{K}\sin\theta}{1 + \sigma^2 K - 2\sigma\sqrt{K}\sin\theta} \quad (1)
\]

where \(a\) is the amplitude transmission, \(\sigma = a \exp(-aL/2)\) is the overall amplitude loss per turn, \(a\) is the loss, \(L\) is the perimeter of the MR, \(K\) is the coupling intensity coefficient, \(\theta = \beta L\) is the single-pass phase shift of the wave propagation, and \(\beta\) is the propagation constant. The propagation constant is obtain from the exact solutions of Helmholtz equations [40, 41],

\[
\left\{ \begin{array}{ll}
U & = 1 + \frac{K'(W)}{UJ_1(U)} \\
V & = 1 + \frac{K'(W)}{n_2^2 W J_1(W)}
\end{array} \right\} \left\{ \begin{array}{ll}
J_1'(U) & = \frac{d}{2} \left( n_2^2 - \beta^2 \right)^{1/2} \\
W & = \frac{d}{2} \beta \left( n_1^2 - n_2^2 \right)^{1/2}
\right. \quad (2)
\]

where \(U = d/2(n_1^2 - \beta^2)^{1/2}\), \(W = d/2(\beta^2 - n_2^2)^{1/2}\), \(V = kd/2(n_1^2 - n_2^2)^{1/2}\), \(d\) is the diameter of the microfibre, \(k\) is the wave number, \(n_1\) and \(n_2\) are RIs of silica and seawater, respectively, which is related to the fibre diameter, wavelength and RI of seawater.

The seawater refractive index follows the following empirical formula [42]:

\[
n(S, T, \lambda) = 1.31405 \\
\quad + (1.779 \times 10^{-4} - 1.05 \times 10^{-6} T + 1.6 \times 10^{-8} T^2) S \\
\quad - 2.02 \times 10^{-6} T + \frac{15.868 + 0.01155 S - 0.00423 T}{\lambda} \\
\quad - \frac{4382}{\lambda^2} + \frac{1.1455 \times 10^{-6}}{\lambda^3} \quad (3)
\]

where \(T\) is the temperature of the seawater, \(S\) is the salinity of the seawater, \(\lambda\) is the probing wavelength, and \(n\) is the refractive index of the seawater. The units of them are °C, %o, nm and RIU (Refractive Index Unit), respectively.

3 NUMERICAL RESULTS

Based on the above theory, we calculate the resonant spectrum of the MR in seawater firstly, as shown in Figure 2(a). In simulations, we assume that the fibre diameter is 1.5 μm, ring diameter is 400 μm, and the salinity of seawater is 35‰. Since the salinity also influences the resonant spectrum, we assume the salinity to be a constant. As shown in Figure 2(a), with the increasing of seawater temperature, the resonant peaks shift due to the RI change of seawater. It can be estimated that the sensitivity of resonant-wavelength-shift scheme is about 0.030 nm/°C. When the resolution of spectral analyzer we used (Ando AQ6370C) is 0.02 nm, the detection limit is estimated to be 0.667°C, which is much lower than that of CTD’s.

For intensity-variation scheme, the sensitivity of the intensity-variation scheme is defined as [38]:

\[
S = \frac{d\tau}{dT} \quad (4)
\]
where $\tau_n$ is the normalized intensity (NI), and $t$ is the temperature of the seawater. To evaluate the sensing sensitivity for intensity-variation scheme, we plot the normalized intensity as a function of the temperature shown in Figure 2(b). In simulations, we choose the wavelength of 1556.312 nm as the probing wavelength which is the resonant peak. It can be seen from Figure 2(b) that the range of normalized intensity between 0 and 0.8 shows the good linear relationship, so we select this linear range to estimate the sensitivity of intensity-variation scheme, and the slope of the fitted line is considered to be the sensing sensitivity. By this method, the estimated sensitivity shown in Figure 2(b) is about 0.2709 NI/°C.

Besides the sensitivity, the detection limit $R$ is another parameter that can evaluate the performance of the system. The detection limit of the system is the smallest change of the temperature that can be detected. The change of temperature effects on the change of the normalization transmission intensity, so the detection limit can be expressed as [38]:

$$R = \frac{\Delta \tau_n}{S}, \quad (5)$$

where $\Delta \tau_n$ is the detectable smallest change of the normalized transmission intensity. The detection limit is influenced by the resolution ratio of the instrument, besides the sensitivity. When the resolution of the power meter we used (Newport 918D-IR-OD3) is 0.0004%, the detection limit is $1.48 \times 10^{-5}$°C. Furtherly, the dynamic detection range of the system shown in Figure 2(b) is about 3.38°C. Considering the internal-wave phenomena happens accompany with the temperature fluctuation of about 1.5 – 3.5°C, it is necessary to widen the dynamic detection range of the system by tuning the parameters of system.

In order to expand the dynamic detection range, we decrease the fibre diametre to be 1 µm and keep ring diametre 400-µm. The probing wavelength is chosen to be 1584.376 nm. As is shown in Figure 3(a), the detection range of the intensity-variation scheme extends to be 6.31°C, which is wide enough for internal-wave sensing. Correspondingly, the sensitivity of the system is about 0.1393 NI/°C, which is lower than that of the system in Figure 2(b). This is because that intensity-variation scheme converts the smaller change of the temperature into a large change of the intensity due to the sharp slope near the resonance wavelength. So, if intensity-variation scheme provides a higher sensitivity and a lower detection limit, a narrower dynamic detection range is inevitable. In other words, it is necessary to choose the proper parameters of system according to the real needs. For example, if we want to improve the sensitivity, we can change the system parameters, such as, the probing wavelength to be 1165.08 nm, the fibre diametre to be 1 µm and the ring diametre to be 800 µm. The dependence of the transmission intensity on temperature is shown in Figure 3(b). In this system, the sensitivity is estimated to be 2.556 NI/°C. Correspondingly, the dynamic detection range decreases to be 0.38°C.

To offer more quantitative references for different detection purposes with different sensitivities, we investigate dependences of the sensitivity on the probing wavelength, fibre diametre and ring diameters.

![Graph](image)

**FIG. 3** The normalized intensity as a function of the temperature, the wavelengths are (a) 1584.376 nm and (b) 1165.08 nm.

### 3.1 Dependence of sensitivity on wavelength

Existing research indicates that in resonant-wavelength-shift scheme sensitivity increases with the increasing probing wavelength [5, 7, 21], which dues that the microfibres with larger wavelength have higher fractional power transmitted in the seawater, so they are more sensitive to the variation of ambient RI. However, in intensity-variation scheme, sensitivity is not decided by power fraction transmitted in seawater absolutely.

Figure 4 shows the dependence of sensitivity on the probing wavelength. In simulation, the fibre diametre is assumed to be 1 µm, and the ring diametre is 400 µm. It can be seen obviously that the dependence of the sensitivity on the probing wavelength is not increasing or decreasing, monotonously, which is much different with resonant-wavelength-shift scheme. It can be explained as follows: in intensity-variation scheme, the sensitivity is a combination of the spectral shift of the resonant mode and the slope of the spectral mode profile and thus the Q-factor. The larger losses, especially, the absorption loss from seawater will result in a lower Q-factor. The losses include guiding loss, bending loss and absorption loss. The evolution and competition of these three losses can be obtained in Reference [21]. The inset in Figure 4 plots the dependence of the absorption coefficient in seawater on the probing wavelength. It can be seen that wavelength with larger absorption coefficient corresponds to the lower sensitivity, which indicates that it is necessary to choose the probing wavelengths with low ab-
The dependences of detection limit on wavelength, ring diameter, and fibre diameter compared to sensitivity. The low detection limit is related to short wavelength, large ring diameter. Additionally, there may exist an optimal fibre diameter, with which the detection limit is minimum. If the resolution ratio of the power meter (Newport 918D-IR-OD3) is 0.0004%, the probing wavelength is 1064 nm, the fibre diameter is 0.75 µm, and the MR diameter is 2000 µm, the sensitivity can reach to 13.78 NI/°C, which is lower than that of CTD system and shows great potential in fine measuring of temperature in seawater. To find the optimal performance of the sensor at different temperature, the dependences of sensitivity and detection limit on fibre diameter at some typical temperatures are plotted in Figure 8. The probing wavelength is assumed to be 1310 nm. It can be seen that high sensitivity and low detection limit are related to high temperature, which is due that the change in the RI of seawater decreases the loss at high temperature and thus increases the Q-factor [16]. Additionally, the optimal fibre diameters for high sensitivity and low detection limit are the same at different temperatures,
FIG. 8 The dependences of (a) sensitivity and (b) detection limit on fibre diametre at some typical temperatures.

which indicates that the optimal fibre diametre for MR with the same ring diametre is mainly determined by the probing wavelength.

4 CONCLUSION

In conclusion, we have numerically studied temperature sensing in seawater based on microfibre resonator by intensity-variation scheme. Dependences of the sensitivity on probing wavelength, ring diametre and fibre diametre are investigated. Results show that the sensitivity of temperature sensing is determined by both the fraction of power outside the fibre and the losses induced by bending and absorption. The probing wavelength influences the sensitivity mostly by the absorption loss. Larger absorption loss results in lower sensitivity, which is much different with resonant-wavelength-shift scheme. And the sensitivity increases with the increasing ring diametre due to the decreasing bending loss and increasing Q-factor. In addition, there may exist an optimal fibre diametre, with which the sensitivity is maximized. By tuning the above parameters of system, sensitivity can be tuned from 0.0784 NI/°C to 13.79 NI/°C. Correspondingly, dynamic range changes from 11.77°C to 0.08°C. Additionally, the dependences of detection limit on wavelength, fibre diametre, and ring diametre are also investigated, which are opposite to that of sensitivity. For different temperatures, the dependences of sensitivity and detection limit at some typical temperatures are studied, which shows that high sensitivity and low detection limit are related to high temperature and the optimal fibre diametres for high sensitivity and low detection limit are the same at different temperatures. The calculated detection limit is about $10^{-7}$ °C, which is four orders of magnitude smaller than that of the traditional method. Results shown here are beneficial to find the optimal parameters for the temperature sensors, and offer helpful references for assembling micro-photonics device used in seawater sensing and detection.

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